

Mental methods for addition



Example 2 - think of: 1236 - 415 as 1236 - 400 - 10 - 5 • But in your head say: 1236 836 826 821

<u>Multi-step problems</u>



Multiples & factors

FACTORS are what divides exactly into a number

e.g. Factors of 12 are:

Factors of 18 are:

1	12	
2	6	
3	4	

1	18	
2	9	
3	6	

The common factors of 12 & 18 are: 1, 2, 3, 6, <u>The Highest Common Factor is: 6</u>

 MULTIPLES
 are the times table answers

 e.g. Multiples of 5 are:
 Multiples of 4 are:

 5 10 15 20 25
 4 8 12 16 20

The Lowest Common Multiple of 5 and 4 is: 20

Prime numbers

Prime numbers have only TWO factors

The factors of 12 are:	Factors of 7 are:
1, 2, 3, 4, 6, 12	1, 7
†	†
12 is <u>NOT prime</u>	7 <u>IS prime</u>
It is <u>composite</u>	

Prime numbers to 30

1	2	2 3		5
6	7 8		9	10
11	12	13	14	15
16	17	18	19	20
21	22	23	24	25
26	27	28	29	30

The number '1' is NOT prime



Multiplication using a formal method			method	Division using a formal method		
• By a ONE-DIGIT number			ber	• By a ONE-DIGIT number		
e.g. 3561×7 <u>COLUMN METHOD</u> 3561 $\frac{x}{24927}$ 34			<u>METHOD</u>	e.g. 9138 ÷ 6 <u>1526</u> 6)9³1¹3¹8 • By a TWO-DIGIT number e.g. 4928 ÷ 32 <u>SAME METHOD</u>		
e.g. 3561	l x 7	GRID ME	THOD	(Except write down some of your tables down first) 32		
	3000	500 6	60 7	96 $32\overline{)4^{4}9^{17}2^{12}8}$		
7	21000	3500 4	20 49	128		
21,00	0 + 3,500 +	420 + 49 :	= 24,927	160 4928 ÷ 32 = <u>154</u>		
• By a TWO-DIGIT number e.g. 152×34 <u>COLUMN METHOD</u> 152 $\times 34$ 608 (152×4) 4560 (152×30) 5168			ber METHOD 52 x 4) 52 x 30)	e.g. $4928 \div 32$ <u>ALTERNATE METHOD</u> • Divide • Multiply • Subtract • Bring down - Make a new number • Divide 0 154 32 4928 -32 4 172 -160 4 128 -128 000 $4928 \div 32 = 154$		
	100	50	2			
30	3000	1500	60	Place Value		
י 152 x 34	= 3400 +	1700 + 6	58 = <u>5168</u>	Matimum HTH TTH TH Image: Margin and State an		

Multiply & divide by 10, 100, 1000

• By moving the digits

To multiply by 10 move the digits ONE place LEFT

e.g.

3.52 × 10

To multiply or divide by 100 move TWO places To multiply or divide by 1000 move THREE places

• By moving the decimal point To multiply by 10 move the dp ONE place RIGHT

e.g. $13^{1} \times 10 = 130$ $3.4 \times 10 = 34$

To divide by 10 move the dp ONE place LEFT

e.g.
$$13 \div 10 = 1.3$$

 $\sqrt{3}.4 \div 10 = 0.34$

Square & Cube numbers



The first 12 square numbers are: 1, 4, 9, 16, 25, 36, 49, 64, 81, 100, 121, 144



The first 10 cube numbers are: 1, 6, 27, 64, 125, 216, 343, 512, 729, 1000

Equivalent fractions

These fractions are the same but can be drawn and written in different ways



$\frac{3}{4}$	=	$\frac{12}{16}$
$\frac{3^{(x4)}}{4^{(x4)}}$	=	$\frac{12}{16}$

Fractions can also be divided to make the fraction look simpler - this is called CANCELLING or LOWEST FORM

$$\frac{12}{16} \stackrel{(\div 4)}{(\div 4)} = \frac{3}{4}$$



Fractions





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\frac{3}{4} \times 3 = \frac{3}{4} + \frac{3}{4} + \frac{3}{4} = \frac{9}{4} = 2\frac{1}{4} \\
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OR
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OR
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Read & write decimals

The position of the digit gives it its value.

hundreds	tens	units	•	tenths	hundredths	thousandths
3	5	2	•	6	1	7
300	50	2		$\frac{6}{10}$	$\frac{1}{100}$	$\frac{7}{1000}$
352		352		$\frac{6}{10}$	51 00	$\frac{7}{1000}$
352				$\frac{617}{1000}$	-	

Order decimals

Example - To order 0.28, 0.3, 0.216

- Write them under each other
- Fill gaps with zeros
- Then order them

smallest largest Order: 0.216 0.28 0.3

Round decimals

- 1. Find the 'round off' digit
- 2. Move one digit to its right
- Is this digit 5 or more
 Yes add one to the round off digit
 No don't change the round off digit

e.g. 1 - To round 5 .62 to the nearest whole				
'round off' digit this digit is 5 or more				
5.62 rounded to nearest whole = 6				
e.g. 2 - To round 5 .32 to the nearest whole				
'round off' digit this digit is NOT 5 or more				
5.32 rounded to nearest whole = 5				
• To one decimal place				
e.g. 1 - To round 12. <mark>37</mark> to 1 decimal place				
'round off' digit this digit is 5 or more				
12.37 rounded to 1dp = 12.4				
e.g. 2 - To round 12.32 to the nearest whole				
'round off' digit this digit is NOT 5or more				
12.37 rounded to 1dp = 12.3				

• To the nearest whole number

Decimal & Percentage equivalents

Learn

Fraction	Decimal	Percentage	
$\frac{1}{2}$	0.5	50%	
$\frac{1}{4}$	0.25	25%	
$\frac{1}{5}$	0.2	20%	
$\frac{1}{10}$	0.1	10%	
$\frac{1}{100}$	0.01	1%	

Some fractions have to be changed to be 'out of 100'

 $\frac{11}{25}_{(\times 4)}^{(\times 4)} = \frac{44}{100} = 0.44 = 44\%$

<u>Convert metric measure</u>

• Length





• Capacity or volume



Imperial measure

• 1 inch is about 2.5cm



• 1km = 1.6 miles or 5miles = 8km



• 1kg is about 2.2pounds



 A litre of water is a pint and three quarters



• A gallon is about 4.5 litres



<u>Area & Perimeter</u>

• Estimate area

The area is the space something takes up



Number of whole squares(\bigcirc = 16

Number of $\frac{1}{2}$ or more (\times) = 5

<u>Estimated area = 21 squares</u>



• Shapes composed of rectangles

Put on all missing lengths first For **perimeter** - **ADD** all lengths around outside For **area** - split into rectangles & add them together



<u>Perimeter = 12 + 6 + 4 + 2 + 8 + 4 = 36cm</u>



Area of shape = Area of A + B = (8x4) + (6x4) = 32 + 24 <u>Area = 56cm²</u>

<u>Volume</u>



2D representations of 3D shapes



<u>Angles</u>

• Types of angles

Acute (less than 90°) **Obtuse** (Between 90° & 180°)





• Measure and draw angles



To be sure, count the number of degrees between the two arms of the angle



Reflection

• Reflection in a vertical line



• Reflection in a horizontal line



Translation – 4 right & 1 down



- In reflection and translation the shapes remain the same size and shape -CONGRUENT
- In reflection the shape is flipped over
- In translation the shape stays the same way up

Data Handling and statistics

<u>Line graphs</u>

• Find the difference

<u>Example 1</u>: What was the difference in temperature between 1030 and 1130?

<u>Answer</u>: $11.5^{\circ}C - 10^{\circ}C = 1.5^{\circ}C$



• Find the sum of the data

<u>Example</u>: What was the total number of days absent over the 6 years?

<u>Answer</u>: 3 + 4 + 7 + 7 + 9 + 2 = 32 days



Interpret information in tables

• Distance table

Example: Find the distance between Leeds and York Answer: 40miles



• Timetable

Example: How long is the film? Answer: 1.10 - 2.35 = 1h 25min = 85min

6.30am	Educational programme
7.00	Cartoons
7.25	News and weather
8.00	Wildlife programme
9.00	Children's programme
11.30	Music programme
12.30pm	Sports programme
1.00	News and weather
1.10 - 2.35pm	Film

• Table of results of goals scored

Example: Did boys or girls score the most goals? Answer: Boys: 6+3+3+6=18 Girls: 7+5=12

Boys scored the most goals

	Game 1	Game 2	Game 3	Game 4	Game 5	Frequency
Peter	1	0	0	2	3	6
John	0	2	1	0	0	3
Ryan	1	0	1	1	0	3
Claire	2	0	2	1	2	7
Bill	3	1	1	0	1	6
Susan	0	1	3	1	0	5

Times tables and associated facts

If we know $6 \times 7 = 42$ we also can know:

$$42 \div 6 = 7$$

42 ÷ 7 = 6

70 × 6 = 420

60 × 7 = 420

60 x 70 = 4200

70 x 60 = 4200

420 ÷ 6 = 70

420 ÷ 60 = 7

420 ÷ 7 = 60

 $420 \div 70 = 6$

 $0.7 \times 6 = 4.2$

7 x 0.6 = 4.2

0.7 x 0.6 = 0.42 etc

Always try to spot patterns in maths... it makes things a lot easier.